



AKADEMIA EDUKACYJNO - INŻYNIERSKA

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MATURA STUDIA PRAKTYKA STAŻ PRACA BIZNES PRZEMYSŁ STEAM

KOMPLEKSOWE WSPARCIE EDUKACYJNE ON – LINE NA KAŻDYM ETAPIE KSZTAŁCENIA INŻYNIERSKIEGO

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MECHANIKA II

"KINEMATYKA MECHANIZMÓW – RUCH POSTĘPOWY, OBROTOWY, PŁASKI"

PROJEKT

Oblicz:

- prędkość liniową
- prędkość kątową
- przyspieszenie liniowe
- przyspieszenie kątowe

punktów węzłowych oraz każdego członu mechanizmu płaskiego w danym położeniu i danej chwili czasu.

DANE:

$$l, \varphi_l, \omega_l, \varepsilon_l = OK$$

SZUKAM:

$$V, \omega, a, \varepsilon = ?$$

$$D: |AB|, |BC|, |CD| = \checkmark$$

$$N_1 = \checkmark$$

$$v_B = v_A + \omega_1 \cdot |AB|$$

$$v_B = v_A = \omega_1 \cdot |AB| = \checkmark$$

$$v_B = v_{B02} + v_{B01} \quad ??$$

$$v_B = v_{B02} = \omega_2 \cdot |B02|$$

$$\omega_2 = \frac{v_B}{|B02|} \quad ?$$

$$v_C = v_{C02} + v_{C01} \quad ??$$

$$v_C = v_{C02} = \omega_2 \cdot |C02| = \checkmark$$

$$\omega_1 = \checkmark$$

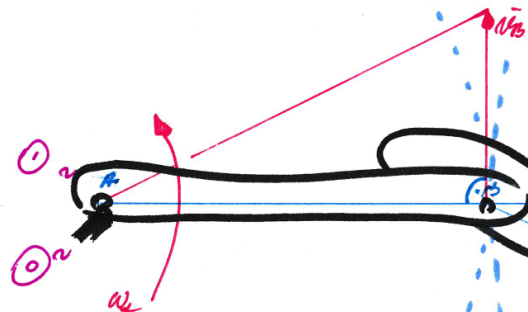
$$v_B = \omega_1 \cdot |AB| = \checkmark$$

$$\omega_2 = \frac{v_B}{|B02|} = \frac{\omega_1 \cdot |AB|}{\sqrt{|AB|^2 - |C02|^2}}$$

$$v_C = \dots \omega_2$$

$$v_C = \omega_2 \cdot |C02| = \checkmark$$

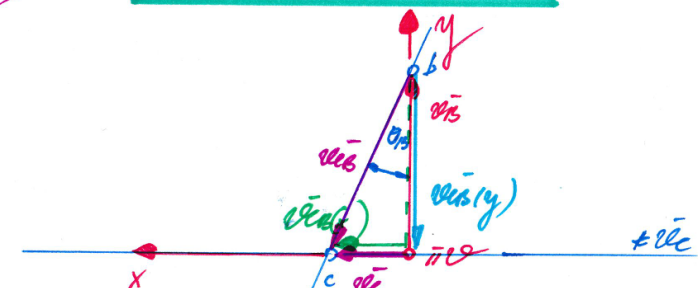
$$v_{C01} = \frac{\omega_2 \cdot |AB|}{\cos \theta_B}$$



$$|BC|^2 = |B02|^2 + |C02|^2$$

$$|B02| = \dots$$

$$v_C = v_{CB} + v_{CS} \quad ?$$



$$\sin \theta_B = \frac{|C02|}{|BC|}$$

$$\theta_B = \arcsin \left(\frac{|C02|}{|BC|} \right)$$

$$v_C = v_{CB} + v_{CS}$$

$$v_C = 0 + v_{CS}(x)$$

$$0 = v_B - v_{CS}(y)$$

$$v_C = v_{CB} \sin \theta_B$$

$$v_B = v_{CB} \cos \theta_B \quad (2?)$$

$$v_C = v_{CB} \sin \theta_B$$

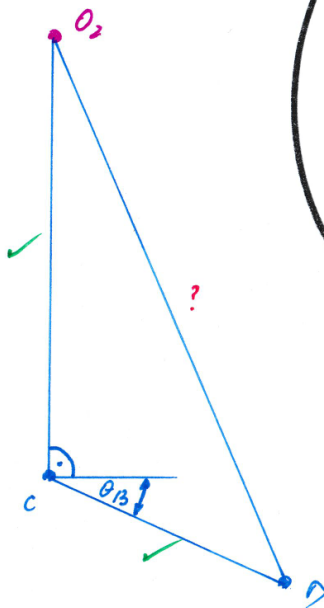
$$v_{CB} = \frac{v_B}{\cos \theta_B}$$

$$v_C = \frac{v_B}{\cos \theta_B} \sin \theta_B = v_B \tan \theta_B$$

un?

$$\vec{v}_D = \vec{v}_{O_2} + \vec{v}_{DO_2}$$

$$\Rightarrow \underline{v_D} = v_{DO_2} = \omega_2 \cdot |DO_2| = ?$$



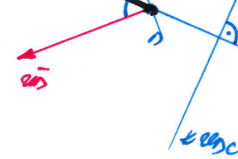
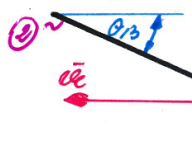
$$|DO_2| = \sqrt{|CO_2|^2 + |CO_2|^2 - 2|CO_2||CO_2|\cos(90^\circ + \theta_B)}$$

$$\Rightarrow \underline{|DO_2|} = \checkmark$$

$$\Rightarrow \underline{v_D} = \omega_2 \cdot |DO_2| = \checkmark$$

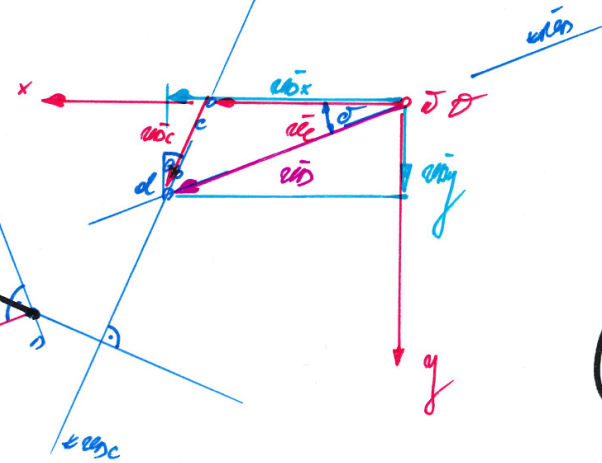
un?

$$\vec{v}_D = \vec{v}_C + \vec{v}_{DC}$$



$$\frac{v_{Dx}}{v_D} = \cos \gamma \quad | \quad \text{and}(\dots)$$

$$\gamma = \arcsin\left(\frac{v_{Dx}}{v_D}\right)$$



$$x) \quad v_{Dx} = v_C + v_{Dc} \sin \theta_B$$

$$y) \quad v_{Dy} = 0 + v_{Dc} \cos \theta_B$$

$$\Rightarrow \underline{v_{Dc}} = \omega_2 \cdot |DC| = \checkmark$$

$$x) \quad v_{Dx} = v_C + v_{Dc} \sin \theta_B$$

$$y) \quad v_{Dy} = v_{Dc} \cos \theta_B$$

$$v_D = \sqrt{v_{Dx}^2 + v_{Dy}^2}$$

$\triangleright: |AB|, |AD|, |BC| = \checkmark$
 $\omega_1, \underline{e}_1 = \checkmark$

$\underline{\bar{a}}_B = \underline{\bar{a}}_A + \underline{\bar{\omega}}_1 \underline{r}_{AB} + \underline{\bar{\omega}}_1 \underline{r}_{AB}$

$\underline{\bar{\omega}}_1 = 0 \quad [m/s^2]$

$\underline{\bar{\omega}}_1^u = \omega_1^2 \cdot |AB| = \checkmark$

$\underline{\bar{\omega}}_1^t = \underline{e}_1 \cdot |AB| = \checkmark$

$\underline{\bar{r}} = \underline{\bar{\omega}} \cdot \underline{a} = \frac{\underline{\bar{\omega}} \cdot \underline{v}^2}{r}$

$\underline{\bar{a}} = \frac{\omega^2 \underline{e}^t}{r} = \omega^2 \underline{e}$

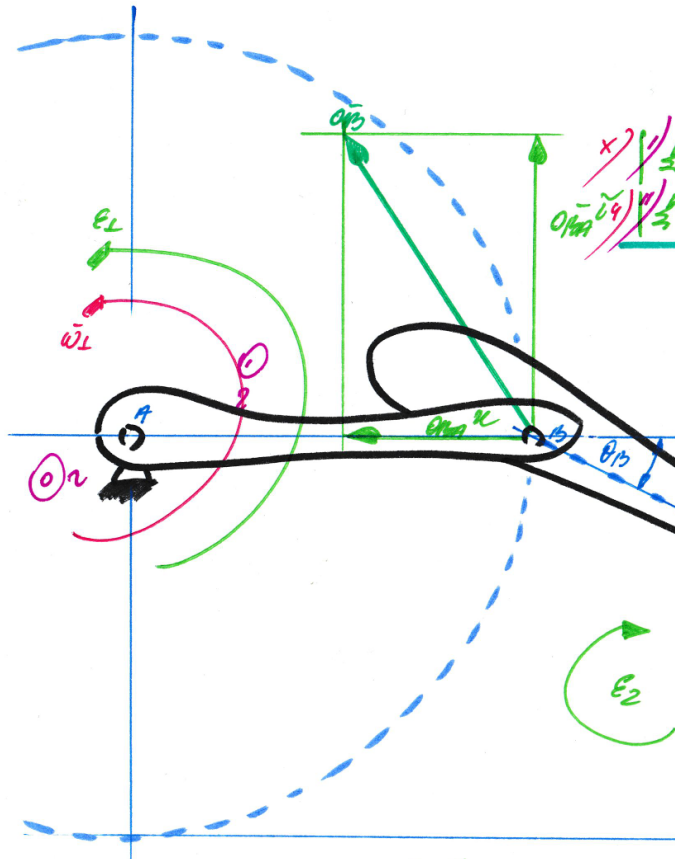
$? \underline{\bar{a}}_C = \underline{\bar{a}}_B + \underline{\bar{\omega}}_2 \underline{r}_{BC} + \underline{\bar{\omega}}_2 \underline{r}_{BC}?$

$\underline{\bar{\omega}}_2 = \checkmark$

$\underline{\bar{\omega}}_2^u = \omega_2^2 \cdot |CB| = \checkmark$

$\underline{\bar{\omega}}_2^t = \underline{e}_2 \cdot |CB| = ? ; \underline{e}_2 = ?$

$\underline{\bar{\omega}}_2 = \text{Hör. Hör.}$

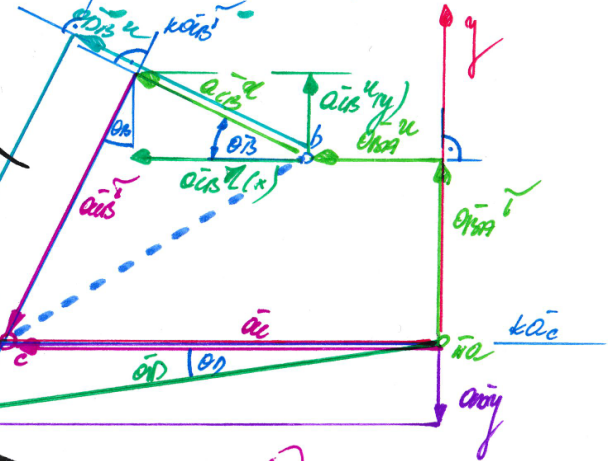


$\frac{1}{2} \underline{\bar{a}}_x = \underline{\bar{a}}_C = \underline{\bar{\omega}}_1^u + \underline{\bar{\omega}}_2^u \cos \theta_B + \underline{\bar{\omega}}_2^t \sin \theta_B$
 $\frac{1}{2} \underline{\bar{a}}_y = 0 = \underline{\bar{\omega}}_1^t + \underline{\bar{\omega}}_2^u \sin \theta_B - \underline{\bar{\omega}}_2^t \cos \theta_B$

$\underline{\bar{a}}_C = \checkmark$
 $\underline{\bar{\omega}}_2^t = \checkmark$

$\underline{\bar{\omega}}_2^t = \underline{e}_2 \cdot |CB|$

$\underline{e}_2 = \frac{\underline{\bar{\omega}}_2^t}{|CB|}$



$\underline{\bar{a}}_D = \underline{\bar{a}}_B + \underline{\bar{\omega}}_2 \underline{r}_{BD} + \underline{\bar{\omega}}_2 \underline{r}_{BD}$

$\underline{\bar{\omega}}_2 = \checkmark ; \underline{\bar{\omega}}_2^t = \underline{e}_2 \cdot |DB| = \checkmark$

$\underline{\bar{\omega}}_2^u = \omega_2^2 \cdot |DB| = \checkmark$

$\frac{1}{2} \underline{\bar{a}}_x = \underline{\bar{a}}_D = \underline{\bar{\omega}}_2^u + \underline{\bar{\omega}}_2^u \cos \theta_D + \underline{\bar{\omega}}_2^t \sin \theta_D$
 $\frac{1}{2} \underline{\bar{a}}_y = \underline{\bar{a}}_y = \underline{\bar{\omega}}_2^t + \underline{\bar{\omega}}_2^u \sin \theta_D - \underline{\bar{\omega}}_2^t \cos \theta_D$

$\underline{\bar{a}}_D = \sqrt{(\underline{\bar{a}}_x)^2 + (\underline{\bar{a}}_y)^2} = \checkmark$

$\frac{\underline{\bar{a}}_x}{\underline{\bar{a}}_D} = \cos \theta_D \Rightarrow \theta_D = \arccos \left(\frac{\underline{\bar{a}}_x}{\underline{\bar{a}}_D} \right)$

