



AKADEMIA EDUKACYJNO - INŻYNIERSKA

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MATURA STUDIA PRAKTYKA STAŻ PRACA BIZNES PRZEMYSŁ STEAM

KOMPLEKSOWE WSPARCIE EDUKACYJNE ON – LINE NA KAŻDYM ETAPIE KSZTAŁCENIA INŻYNIERSKIEGO

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MECHANIKA II

"DYNAMIKA PUNKTU MATERIALNEGO"

PROJEKT

Oblicz:

- kąt początkowy
- czas całkowity

nachylenia i lotu strzały wypuszczonej przez strzelca, aby trafiła ona w spadający z palmy ananas.

DANE:

$$d, h = OK$$

SZUKAM:

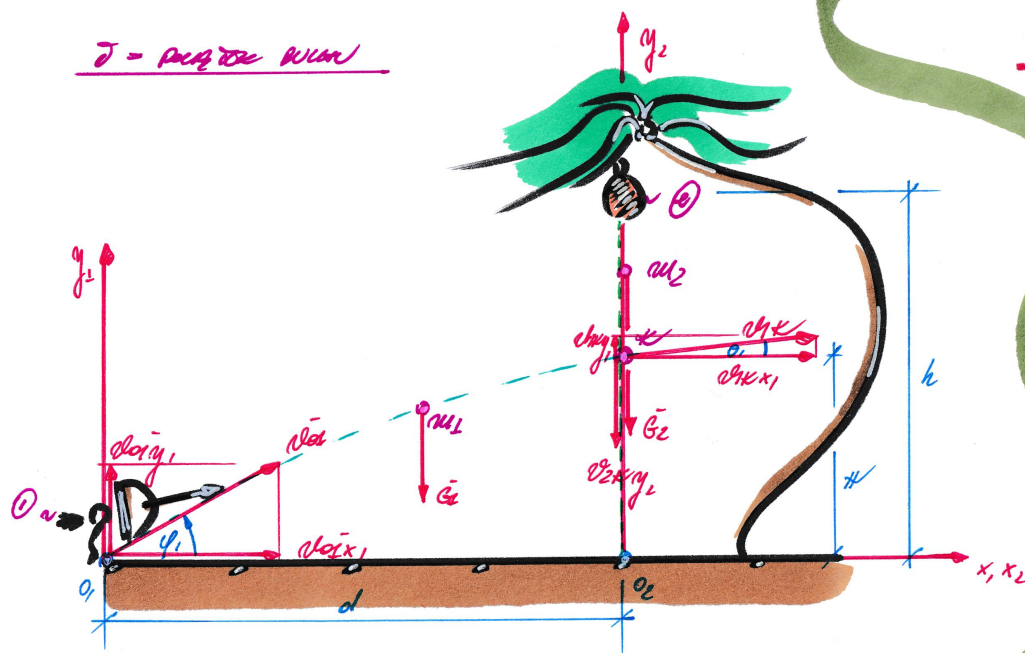
$$\varphi_{0I}, T = ?$$

9.6

$d, k = \checkmark$

$\bar{d} = \text{position when}$

$\varphi_1, \bar{d} = ?$



$\bar{d} = m \cdot \bar{a}$

$x_1(t), y_2(t)$

$$\begin{aligned} \sum F_{x1} &= m_1 \ddot{x}_1 = 0 \\ \sum F_{y2} &= m_2 \ddot{y}_2 = -\bar{G}_2 \end{aligned}$$

$$1) m_1 \ddot{x}_1 = 0 \quad | : m_1$$

$$\begin{aligned} \ddot{x}_1(t) &= 0 \\ \dot{x}_1(t) &= C_1 \\ x_1(t) &= C_1 t + C_2 \end{aligned}$$

$$\begin{aligned} \dot{x}_1(t=0) &= \dot{x}_{01} = \dot{x}_0 \cos \varphi_1 \\ x_1(t=0) &= x_{01} = 0 \end{aligned}$$

$$\begin{aligned} C_1 &= \dot{x}_0 \cos \varphi_1 \\ C_2 &= 0 \end{aligned}$$

$$\begin{aligned} \ddot{x}_1(t) &= 0 \\ \dot{x}_1(t) &= \dot{x}_0 \cos \varphi_1 \\ x_1(t) &= \dot{x}_0 t \cos \varphi_1 \end{aligned}$$

$\bar{d} = \text{max when } \dot{d} = 0$

$$\begin{aligned} \dot{x}_1(t=\bar{d}) &= \dot{x}_0 \cos \varphi_1 \\ x_1(t=\bar{d}) &= d \\ \dot{y}_2(t=\bar{d}) &= \dot{x}_0 \sin \varphi_1 \\ y_2(t=\bar{d}) &= \bar{d} \end{aligned}$$

$$1) m_2 \ddot{y}_2 = -\bar{G}_2$$

$$m_2 \ddot{y}_2 = -m_2 g$$

$$\ddot{y}_2(t) = -g$$

$$\dot{y}_2(t) = -gt + C_3$$

$$y_2(t) = -\frac{1}{2}gt^2 + C_3 t + C_4$$

$$\dot{y}_2(t=0) = \dot{y}_{02} = \dot{x}_0 \sin \varphi_1$$

$$y_2(t=0) = y_{02} = 0$$

$$C_3 = \dot{x}_0 \sin \varphi_1$$

$$C_4 = 0$$

$$\begin{aligned} \ddot{y}_2(t) &= -g \\ \dot{y}_2(t) &= -gt + \dot{x}_0 \sin \varphi_1 \\ y_2(t) &= -\frac{1}{2}gt^2 + \dot{x}_0 t \sin \varphi_1 \end{aligned}$$

$$\begin{aligned} \dot{x}_1 &= \dot{x}_0 \cos \varphi_1 \\ d &= \dot{x}_0 \bar{d} \cos \varphi_1 \\ \dot{y}_2 &= -g \bar{d} + \dot{x}_0 \sin \varphi_1 \\ \bar{d} &= -\frac{1}{2}g \bar{t}^2 + \dot{x}_0 \bar{t} \sin \varphi_1 \end{aligned}$$

$$1) \ddot{y}_2 = -g$$

$$\ddot{y}_2 = -g$$

$$y_2(t) = -gt + C_5$$

$$y_2(t) = -\frac{1}{2}gt^2 + C_5t + C_6$$

$$y_2(t) = -\frac{1}{2}gt^2 + C_5t + C_6$$

$$y_2(t=0) = 0$$

$$y_2(t=0) = h = y_{02}$$

$$C_5 = 0$$

$$C_6 = h$$

$$y_2(t) = -gt$$

$$y_2(t) = -gt$$

$$y_2(t) = -\frac{1}{2}gt^2 + h$$

$$\tau = \text{const} \text{ when } d \text{ is const}$$

$$y_2(t=\tau) = -v_2 \tau$$

$$y_2(t=\tau) = h$$

$$-v_2 \tau = -g\tau$$

$$-\frac{1}{2}g\tau^2 + h = h$$

3?

$$1) \ddot{y}_2 = -g$$

$$d = \frac{d}{dt} \tau \cos \varphi_1$$

$$\ddot{y}_2 = -g\tau + \frac{d}{dt} \tau \sin \varphi_1$$

$$\ddot{y}_2 = -\frac{1}{2}g\tau^2 + \frac{d}{dt} \tau \sin \varphi_1$$

4?

$$2) \ddot{y}_2 = -g\tau$$

$$-\frac{1}{2}g\tau^2 + h = h$$

$$\tau \sin \varphi_1 = \frac{h}{d}$$

$$d = \frac{d}{dt} \tau \cos \varphi_1$$

$$\tau = \frac{d}{\cos \varphi_1}$$

$$11, 11)$$

$$h = -\frac{1}{2}g\tau^2 + \frac{d}{dt} \tau \sin \varphi_1 = -\frac{1}{2}g\tau^2 + \frac{h}{\cos \varphi_1} \cdot \sin \varphi_1$$

$$-g\tau^2 + 2 \frac{d}{dt} \tau \sin \varphi_1 = -g\tau^2 + h$$

$$2 \frac{d}{dt} \tau \sin \varphi_1 = h$$

$$2 \frac{d}{dt} \left(\frac{d}{\cos \varphi_1} \right) \cdot \sin \varphi_1 = h$$

$$2 d \sin \varphi_1 = h$$

$$\sin \varphi_1 = \frac{h}{2d}$$

$$\varphi_1 = \arcsin \left(\frac{h}{2d} \right)$$

