



AKADEMIA EDUKACYJNO - INŻYNIERSKA

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MATURA STUDIA PRAKTYKA STAŻ PRACA BIZNES PRZEMYSŁ STEAM

KOMPLEKSOWE WSPARCIE EDUKACYJNE ON – LINE NA KAŻDYM ETAPIE KSZTAŁCENIA INŻYNIERSKIEGO

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MECHANIKA II

"DYNAMIKA - UKŁAD BRYŁ SZTYWNYCH"

PROJEKT

Oblicz:

- przyspieszenie "2"
- siłę tarcia
- siłę w linie

dla układu brył sztywnych.

DANE:

1) $m_1, r_1 = OK$

2) $m_2 = OK$

SZUKAM:

$$x_2''(t) = ?$$

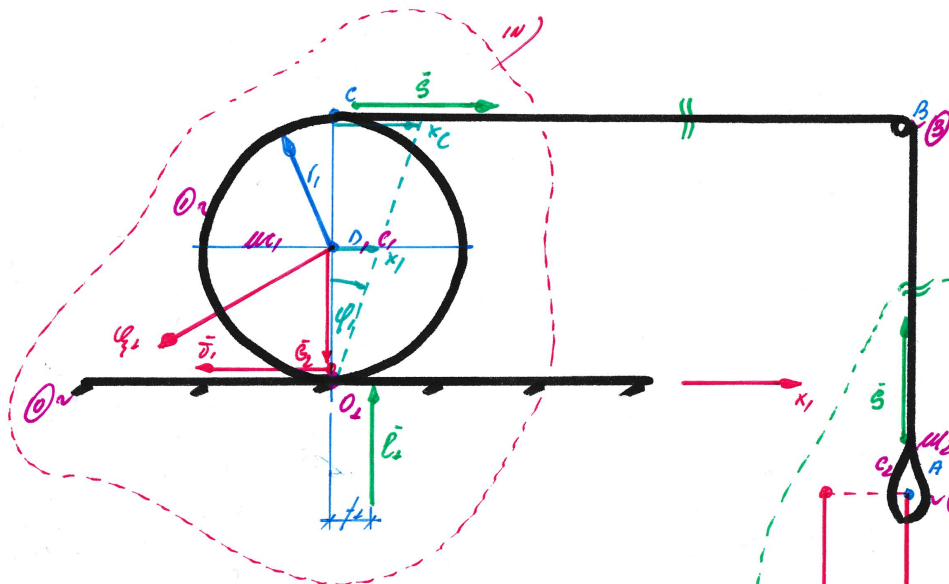
5.6)

$$m_1 = m$$

$$r_1 = R$$

$$\ddot{x}_2(t) = ?$$

$$m_2 = M$$



$$\begin{cases} \vec{F} = m \cdot \vec{a} \\ \vec{M} = \vec{I} \cdot \vec{\epsilon} \end{cases}$$

$$\begin{aligned} \text{i)} \quad & \frac{1}{2} F x_1 = m \ddot{x}_1 = \ddot{s} - \ddot{\tau}_1 \\ & \frac{1}{2} F y_1 = m_1 \ddot{y}_1 = \ddot{\epsilon}_1 - \ddot{G}_1 \\ & \frac{1}{2} M \ddot{\phi}_1 = \vec{I}_1 \ddot{\phi}_1 = \vec{\tau}_1 \cdot \vec{r}_1 - \vec{L}_1 \cdot \vec{t}_1 \end{aligned}$$

$$\text{e)} \quad \frac{1}{2} F x_2 = m_2 \ddot{x}_2 = \ddot{\epsilon}_2 - \ddot{s}$$

$$\text{ii)} \quad L_1 = G_1 = m_1 g$$

$$\vec{I}_1(\vec{e}_1) = \frac{1}{2} m_1 r_1^2$$

$$G_2 = m_2 g$$

$$\begin{aligned} \text{i)} \quad & m_1 \ddot{x}_1 = \ddot{s} - \ddot{\tau}_1 \\ \text{ii)} \quad & \frac{1}{2} m_1 r_1^2 \ddot{\phi}_1 = \ddot{\tau}_1 r_1 - m_1 g t_1 \\ \text{iii)} \quad & m_2 \ddot{x}_2 = m_2 g - \ddot{s} \end{aligned}$$

$$q = \ddot{x}_2$$

$$\ddot{x}_2 = \ddot{\phi}_1 \cdot 2r_1 \Rightarrow \ddot{\phi}_1 = \frac{\ddot{x}_2}{2r_1}$$

$$\ddot{x}_1 = \ddot{\phi}_1 \cdot r_1 = \frac{\ddot{x}_2}{2r_1} \cdot r_1 = \frac{1}{2} \ddot{x}_2$$

$$\begin{aligned} \text{i)} \quad & \frac{1}{2} m_1 \ddot{x}_2 = \ddot{s} - \ddot{\tau}_1 \\ \text{ii)} \quad & \frac{1}{2} m_1 r_1^2 \cdot \frac{\ddot{x}_2}{2r_1} = \ddot{\tau}_1 r_1 - m_1 g t_1 \\ \text{iii)} \quad & m_2 \ddot{x}_2 = m_2 g - \ddot{s} \end{aligned}$$

$$\begin{aligned} \text{i)} \quad & \frac{1}{2} m_1 \ddot{x}_2 = \ddot{s} - \ddot{\tau}_1 \\ \text{ii)} \quad & \frac{1}{4} m_1 r_1 \ddot{x}_2 = \ddot{\tau}_1 r_1 - m_1 g t_1 \\ \text{iii)} \quad & m_2 \ddot{x}_2 = m_2 g - \ddot{s} \end{aligned}$$

$$\frac{1}{2} m_1 \ddot{x}_2 = \ddot{s} - \ddot{\tau}_1$$

$$\begin{aligned} \text{iv)} \quad & m_2 \ddot{x}_2 = m_2 g - \ddot{s} \\ \Rightarrow \quad & \ddot{s} = m_2 g - m_2 \ddot{x}_2 \end{aligned}$$

$$\begin{aligned} \text{iii)} \quad & \frac{1}{4} m_1 r_1 \ddot{x}_2 = \ddot{\tau}_1 r_1 - m_1 g t_1 \\ \Rightarrow \quad & \ddot{\tau}_1 = \frac{0.25 m_1 r_1 \ddot{x}_2 + m_1 g t_1}{r_1} \end{aligned}$$

$$i) \quad \frac{1}{2} m_1 \ddot{x}_2 = 5 - T_2$$

$$\frac{1}{2} m_1 \ddot{x}_2 = m_2 g - m_2 \ddot{x}_2 - 0,25 m_1 \ddot{x}_2 - \frac{m_1 g t_1}{r_2}$$

$$0,5 m_1 \ddot{x}_2 + m_2 \ddot{x}_2 + 0,25 m_1 \ddot{x}_2 = m_2 g - \frac{m_1 g t_1}{r_2}$$

$$(0,75 m_1 + m_2) \ddot{x}_2 = m_2 g - \frac{m_1 g t_1}{r_2}$$

$$\ddot{x}_2(t) = \frac{m_2 g - \frac{m_1 g t_1}{r_2}}{0,75 m_1 + m_2} = \left(\frac{m_2 - \frac{m_1 t_1}{r_2}}{0,75 m_1 + m_2} \right) g$$

$$ii) \quad T_2 = 0,25 m_1 \ddot{x}_2 + \frac{m_1 g t_1}{r_2}$$

$$iii) \quad S_k = m_2 g - m_1 \ddot{x}_2$$

